

Personalized federated prototype learning in mixed heterogeneous data scenarios

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Abstract. Federated learning has received significant attention for its ability to s imultaneously protect customer privacy and leverage distributed data from multiple devices for model training. However, conventional approaches often focus on isolated heterogeneous scenarios, which results in skewed feature distributions or label distributions. Meanwhile, data heterogeneity is actually a key factor in improving model performance. To address this issue, we propose a new approach called PFPL in mixed heterogeneous scenarios. The method provides richer domain knowledge and unbiased convergence targets by constructing personalized, unbiased prototypes for each client. Moreover, in the local update phase, we introduce consistent regularization to align local instances with their personalized prototypes, which significantly improves the convergence of the loss function. Experimental results on Digits and Office Caltech datasets validate the effectiveness of our approach and successfully reduce the communication cost.

Keywords: Skewed label distribution, Skewed distribution of features, Personalized Federal Learning, data heterogeneity.

1 Introduction

The rapid proliferation of mobile phones, wearables, tablets, and smart home devices has led to exponential growth in the volume of data generated and retained by these de vices [1,2]. These data contain valuable insights for device owners. However, many us ers have become increasingly concerned about privacy, demanding that their data rem ain exclusively on local devices. Federated Learning (FL) [3] provides a privacy-prese rving distributed machine learning framework. In FL, a cloud server coordinates with distributed clients while ensuring data privacy through localized storage. The foundati onal FedAvg algorithm [4] iteratively aggregates client model parameters and distributes averaged global models to clients, enabling collaborative training without privacy disclosure. However, real-world scenarios involve data from heterogeneous sources w

ith distinct characteristics, resulting in non-independent and identically distributed (no n-IID) data [5,6]. Local client updates based on their data distributions often diverge f rom the global optimization trajectory. Personalized Federated Learning (PFL) has em erged as a prominent approach to developing client-specific models tailored to individ ual data distributions.

Personalized Federated Learning (PFL) addresses data heterogeneity by enabling cl ients (e.g., mobile devices or organizations) to develop customized models aligned wit h their unique data distributions [7]. Two fundamental challenges persist: (1) label distribution skew across clients, and (2) feature distribution divergence within identical la bel classes. Existing research predominantly focuses on single-mode heterogeneity (ei ther label or feature skew), with limited exploration of cross-domain mixed heterogeneity where data originates from divergent domains with varying label distributions.

Under label skew conditions, the global model exhibits bias toward majority classe s, leading to suboptimal generalization of personalized models on local client data. W hile hybrid local-global optimization [8] and model decoupling techniques [9] show ef ficacy in handling label skew, they fail to address feature distribution bias as the globa l model struggles to capture client-specific feature representations—even for data inst ances sharing identical labels across clients [10]. This feature space misalignment furt her hinders effective inter-client model collaboration. In practical cross-domain deplo yments with dual heterogeneity (concurrent label skew and feature divergence), these limitations not only degrade model performance but also hinder real-world applicability. Consequently, developing unified solutions for hybrid heterogeneous scenarios becomes imperative.

Real-world applications frequently exhibit dual heterogeneity scenarios combining label distribution skew and feature distribution divergence, as exemplified by cross-in stitutional CT image analysis where hospitals in different geographic regions possess distinct patient cohorts. This dual heterogeneity arises from two primary factors: (1) fe ature variations caused by discrepancies in medical imaging equipment specifications, and (2) label distribution skew stemming from demographic differences in disease pr evalence across hospital populations.

Building upon prototype learning foundations [9,11], we present Prototypical Feder ated Partial Learning (PFPL), a novel framework for hybrid heterogeneity scenarios. P FPL employs cross-domain Lipschitz-constrained prototype comparison to quantify d omain-specific knowledge relevance. Through adaptive prototype aggregation weight ed by inter-domain similarity metrics, it constructs client-specific prototypes that miti gate dominant domain bias. Furthermore, we introduce Personalized Prototype Align ment (PPA), a regularization mechanism that enforces consistency between local instance embeddings and client-specific prototypes through feature-space distance minimiz ation, ensuring robustness under hybrid heterogeneity. The main contributions of this paper are summarized as follows:

 We propose a novel personalized prototype learning approach aimed at solving the problem of skewed label distribution and skewed feature distribution in hybrid hete rogeneous scenarios.



- To cope with the label distribution imbalance problem, we introduce prototype lear ning to capture domain knowledge and propose a novel aggregation scheme to gene rate personalized prototypes for each client. Meanwhile, in the local update phase, we design personalized unbiased prototype consistency to provide fair and unbiase d target signals by narrowing the feature distance between instance embeddings and personalized prototypes, thus effectively mitigating the impact of feature distribution imbalance on model performance.
- We conduct extensive experiments on Digits and PACS tasks. The experimental res
 ults show that our scheme outperforms some recent federated learning methods in c
 all and heterogeneous scenarios.

2 Related work

2.1 Heterogeneous challenges in federated learning

Data heterogeneity in federated learning primarily manifests as two distinct types [12, 13]: label distribution skew and feature distribution shift [14]. To address label distribution skew, conventional methods often employ label-based dataset partitioning to con struct pseudo-IID distributions, aiming to reduce training bias and enhance model gen eralization. pFedKT [14] achieves personalized-generalized balance through dual kno wledge transfer: (1) local hypernetworks preserve historical personalized knowledge, and (2) contrastive learning propagates updated global knowledge. Other methods like FedProto [15] and FedProc [16] enforce feature-level consistency through prototype a lignment and procedural feature matching, respectively. However, these methods pred ominantly focus on single-domain label skew scenarios while neglecting cross-domain feature shifts in real-world hybrid heterogeneity.

Feature distribution shift poses a distinct challenge, where cross-domain client data leads to suboptimal cross-domain generalization [17]. FedBN [12] addresses feature s hift through client-specific batch normalization layers prior to model aggregation. AD COL [18] and FCCL [19] impose substantial resource overhead, requiring adversarial discriminators and public datasets for cross-client alignment. While FPL [13] mitigate s feature shift via prototype clustering, it prioritizes global model convergence over client personalization. These approaches primarily target isolated feature shift scenarios while neglecting concurrent label distribution skew. Our work addresses hybrid hetero geneity—simultaneous label skew and feature shift—by developing personalized mod els tailored to individual client data characteristics.

2.2 Personalized federated learning

Personalized federated learning is extensively employed to address the data heterogen eity issue in federated learning. This approach enables each client to customize and op timize the personalized model in accordance with the characteristics and requirements of its local data, thereby facilitating more precise localized model training and adaptat ion.

Personalized federated learning has evolved diverse architectural strategies to addre ss data heterogeneity. Among parameter decoupling approaches, Filip Hanzely et al. [11] have proposed a method that generates personalized models for each client by mi xing local and global models to balance the two. FedBABU [20] extends this paradig m through a three-stage process: local body training with fixed random-initialized hea ds, server-side body aggregation, and post-training head fine-tuning for personalizatio n. FedRoD [21] innovates further with a dual-head architecture comprising a shared g eneral head optimized via class-balanced loss and client-specific private heads trained with empirical loss, where only the body and general head participate in aggregation. Prototype-enhanced methods offer complementary solutions. FedNH [22] integrates p rototype-semantic consistency learning to enhance feature discriminability while empl oying head regularization to prevent prototype collapse under class imbalance. This fr amework adopts alternating optimization: frozen-body head updates precede fixed-head body refinements.

However, most of the above personalization methods only consider the heterogene ous problem for a single scenario (skewed label distribution or skewed feature distribution). There are relatively few personalization methods for mixed scenarios of both, which limits the application of federated learning on more diverse non-IID data. Therefore, solving more diverse hybrid heterogeneous problems has become an important challenge for federated learning research.

3 Methodology

3.1 PRELIMINARY

Following typical federated learning [3], there are M participants, and the private data set of the participants is $D_m = \{x_i, y_i\}_{i=1}^{N_m}$, where N_m represents the client side data size. These private data follow different label distributions and come from different domain s. For example, data sets D_i and D_j on two client sides i and j may have different label statistical distributions. This is common for photo classification apps installed on the mobile client side. The server needs to identify many classes $\mathbb{C} = \{\mathbb{C}(1), \dots \mathbb{C}(k), \dots\}$, while each client side only needs to identify a few classes that make up a subset of \mathbb{C} . The class sets may vary from client side to client side, although there is overlap. And the ese private data sets are derived from different domains, resulting in significant differences in the features of the data even if the categories are the same.

Mixed heterogeneous scenarios in federated learning: P_i(x | y) ≠ P_j(x | y),
 (P_i(y) ≠ P_n(y)). There is a skewed feature distribution and a skewed label distribution between private data. Specifically, the label distribution before different client s ides is different, and the data comes from different domains, presenting a unique feature distribution despite the overlap between domains.

In addition, participants agree to share models with the same architecture. We treat the model as two modules:



Feature Extraction Module ϕ (i.e., the embeddings function) transforms the input from the raw feature space to the embedding space, $f(\phi,x) \to h \in R^d$, the sample x coding d-dimensional feature vector $h = f(\phi,x) \in R^d$. Decision Module φ makes classification decisions for the given learning task. $g:(\varphi,h) \to \hat{y} \in \mathbb{C}$ maps feature h to the logits of utput $\hat{y} = g(\varphi,h) \in \mathbb{C}$. So, the label function can be written as: $F(\phi,\varphi) = f(\phi) \cdot g(\varphi)$, and we use ω to represent (ϕ,φ) for short.

Prototypes: Each prototype is the average of the feature vectors of the same class

$$C^{(k)} = \frac{1}{|D^k|} \sum_{(x,y) \in D^k} f(\phi; x).$$
 (1)

where D^k represents the data instances label K, and $|D^k|$ represents the number of data instances label K.

Local Prototypes: We define a feature $C^{(k)}$ to represent the k-th class in \mathbb{C} . For the i-th client, $C^{(k)}$ is the average of the features obtained by inputting samples with the l abel k into the feature extraction module.

$$C_i^{(k)} = \frac{1}{|D_i^k|} \sum_{(x,y) \in D_i^k} f_i(\phi_i; x).$$
 (2)

where D_i^k represents the data samples of class K in the i-th client.

Global Prototypes: For a given class j, the server receives locally computed features with class label j from a group of clients. These local features with labels j are aggregated by taking their average to generate the global feature $\bar{C}^{(j)}$ for class j.

$$\bar{C}^{(k)} = \frac{1}{\aleph^k} \sum_{i \in \aleph^k} \frac{|D_i^k|}{N^k} C_i^{(k)}.$$
 (3)

where $C_i^{(k)}$ represents the local features of class K from the i-th client, \mathbb{N}^k represents the set of clients that have class K, and N^k represents the total number of data instances of all client-side classes label K.

However, the global prototype is not suitable for the mixed heterogeneous scenario in this paper, which mainly has two problems: **1.** A single global prototype blurs the difference between different domains, and it is difficult to learn special knowledge between different domains. **2.** Since the weight parameter of the global prototype is determined by the amount of data in the category sample, the final global prototype is biased towards the dominant user with a large amount of data, which makes it difficult for the client side with few data instances to learn. A simple approach is to build an unbiased prototype; that is, the prototype weight of each client is the same, but this approach still faces the challenge of problem 1, and this approach makes the client side with few

er sample instances benefit but hurts the client side with more sample instances to part icipate in federated learning.

3.2 Personalized federated prototyping learning

We propose a solution for hybrid heterogeneous FL. This paper uses a prototype as the main component for exchanging information at the client side and server level. The framework is shown in Fig.1. The central server receives local prototype sets $\{\Theta(1), \Theta(2), \cdots, \Theta(m)\}$ from m local client sides and then clusters prototypes $\{\Phi(1), \Phi(2), \cdots, \Phi(k), \cdots\}$ of the same category. In a hybrid heterogeneous FL setup, the ese prototype sets overlap but are not the same. Take the handwritten digit data set as an example. The first client side is the recognition numbers 2, 3, 4, from the MNIST d ata set, while the other client side is the recognition numbers 4, 5, from the SYN data set. These are two sets of handwritten digits from different domains, with different sample categories, albeit overlapping. For the prototype category of each client in the cluster, by assigning weights with the L2 distance of the other client-side prototypes, ag gregation generates a personalized prototype specific to the client.

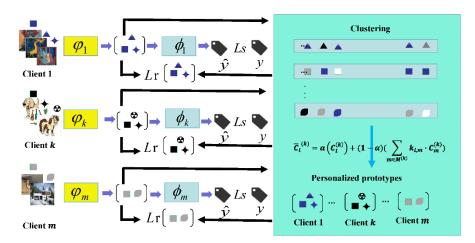


Fig. 1. Architecture of personalized Federated Prototype Learning (PFPL).

Personalized prototype: The server level collects the prototype set of the client and clusters it for the client side prototype category. Taking the prototype with the category K of client side i as an example, its personalized prototype is as follows:

$$\overline{C}_{i}^{(k)} = \alpha(C_{i}^{(k)}) + (1 - \alpha)(\sum_{m \in M^{(k)}} k_{i,m} \cdot C_{m}^{(k)})$$
(4)

where α represents a hyperparameter that controls the degree of personalization, $M^{(k)}$ represents a client side cluster with a K-class label prototype, C_m^k represents the K-class label prototype uploaded by the m client side, and $k_{i,m}$ represents the weight coefficient



nt of the client side m to the i client. The calculation formula is determined by comparing the L2 distance of the two client side K-class prototypes, as follows:

$$k_{i,m} = \frac{\|C_i^{(k)}, C_m^{(k)}\|_2}{\sum_{m \in \Phi(k)} \|C_i^{(k)}, C_m^{(k)}\|_2}$$
(5)

where $\Phi(k)$ represents the cluster prototype with the server level label K, and the L2 d istance between prototypes is calculated as,:

$$\|C_i^{(k)}, C_m^{(k)}\|_2 = \sum_k d(C_i^{(k)} - C_m^{(k)})^2$$
(6)

where d is the locally generated distance metrics of the prototype $C_i^{(k)}$ with label k and prototype $C_m^{(k)}$ with the same label on the other client side m. Distance measures can take many forms, such as L1 distance, L2 distance, and bulldozer distance. Here we use L2 distance metrics.

We generate its personalized prototype for each client side. In simple terms, person alized prototypes with the same label on different clients are affected by domain migration differently. When assigning weight, prototypes from the same domain will assign more weight, while the weight assigned from different domains will be less, making personalized prototypes tend to be more knowledge of the same domain and stay away from the influence of different domains, thus effectively solving the above problem 1 and our weight is determined according to the L2 distance between different client side prototypes, and is not determined by the amount of data on the client side, so it will not be affected by the dominant domain. Although the amount of data on individual prototypes is small, it can also learn more from a large number of prototypes of the same domain, thus solving the problem 2.

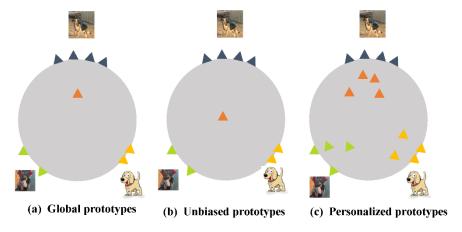


Fig. 2. Description of different prototypes.

Local Model Update: The client side needs to update the local model to generate c onsistent client-side functionality. We also introduce unbiased personalized prototype consistency, which allows the local prototype to approximate its personalized prototype through regularization in local updates. Specifically, the loss function is defined as f ollows:

$$\ell(D_i, w_i) = \ell_S(F(w_i; x_i), y_i) + \lambda \cdot \ell_R\left(\overline{C}_i^{(k)}, C_i^{(k)}\right)$$
(7)

where D_i stands for data from the i-th client, λ is an important parameter for regulariz ation.

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Algorithm 1: PFPL
Input: D_i, w_i, i = 1, \dots m
Output: The final personalization model \{w_i\}, i = 1, \dots, m
      Server executes: (\Theta(i), \overline{C}_i^{(k)})
      Initialize w for all clines
 3:
      for each round T = 1, 2, \cdots do
         for each client i in parallel do
 4:
             \{\Theta(i)\} \longleftarrow \text{LocalUpdate } (i, \overline{C}^{(k)})
 5:
         end for
 6:
 7:
         Clustering prototype sets uploaded by clines
 8:
         Update personalized prototype sets by Eq.(4):
 9:
          Send the personalized prototype to the corresponding
          client side
10:
11:
      end for
      Local Update (i, \overline{C}_i^{(k)}):
12:
      for each local epoch do
13:
14:
         for batch (x_i, y_i) \in D_i do
15:
            Compute local features by Eq.(2)
            Compute loss by Eq.(7) using local prototype
16:
17:
            Update local model according to the loss
            Update local prototype sets \Theta(i) with personalized
18:
            prototypes in \{\bar{C}_{i}^{(k)}\}
19:
          end for
20:
21:
      end for
      return \Theta(i), i = 1,...m
22:
```

Discussion: We further explain the differences between the three prototypes in Fig. 2 The global prototype inherently confuses the knowledge of different domains and s hows a skewed feature space towards the potentially dominant domain in heterogeneous federated learning. Unbiased prototypes also have the problem of confusing the knowledge of the confusion the confusing the knowledge of the confusion the confus



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wledge of different domains, and giving the same weight to the client side with a large number of instance samples is itself an unfair allocation, which reduces the enthusias m of the client side with a large data instance to participate in federated learning. Our personalized prototype solves the above two problems at the same time. Specifically, f or problem 1, our personalized prototype is generated for different client side aggregat es rather than a single global prototype or unbiased prototype, which effectively solve s the problem that the client side data comes from different domains. For problem 2, o ur weight coefficient is mainly determined by hyperparameter a and K, a guarantees th e degree to which our personalized prototype is biased towards the local prototype. Th e calculation formula of K guarantees that other client-side prototypes from the same domain assign more weight, while client-side prototypes from different domains assig n less weight, so that the final personalized prototype is biased towards the real domai n and deviates from other domains. Compared with the traditional model gradient para meter, the dimension of the prototype is much smaller than that of the overall model, which brings less computational cost to the participants. In addition, prototype upload s are privacy-safe because they are one-dimensional vectors generated by averaging lo w-dimensional representations from the same class of samples, which is an irreversible e process. Second, an attacker cannot rebuild the original data source from the prototy pe without accessing the local model. Therefore, prototype not only provides lower co mputational cost, but also a privacy-preserving scheme in heterogeneous federated lea rning.

3.3 Optimization Objective

The goal of PFPL is to solve joint optimization problems on distributed networks. PFP L applies prototype-based communication, which allows a local model to align its local prototype with its personalized prototype while minimizing the sum of losses for all client side local learning tasks. The learning goal of personalized federated prototypes across heterogeneous clients can be expressed as:

$$\underset{\phi,\phi}{\arg\min} \sum_{i=1}^{m} \frac{D_{i}}{N} \ell_{S}(f(w_{i}; x_{i}), y_{i}) + \lambda \cdot \sum_{k=1}^{|C|} \sum_{i=1}^{m} \ell_{R}(\overline{C}_{i}^{(k)}, C_{i}^{(k)}).$$
 (8)

where loss $\ell_s(F(wi; x_i), y_i)$ represents the objective loss for the i-th client, and we use the standard cross-entropy loss as the objective loss function. N represents the sum of all client-side instance data, $|\mathbb{C}|$ represents the number of classes for the labels, and ℓ_R is the regularization term used to measure distance, with its expression as follows:

$$\ell_{R}\left(\bar{C}_{i}^{(k)}, C_{i}^{(k)}\right) = \|\bar{C}_{i}^{(k)}, C_{i}^{(k)}\|_{2} \tag{9}$$

where ℓ_R is the distance metrics of the locally generated prototype $C_i^{(k)}$ and the globally aggregated personalized prototype $\bar{C}_i^{(k)}$. Here we use the L2 distance to measure the difference between the two. The specific algorithm is shown in Algorithm 1.

4 Convergence analysis

We use the first-level model (decision module) as our objective loss function. **Assumption 1.** (Lipschitz Smooth). It is assumed that each local objective function is L_1 -Lipschitz Smooth, which also implies that the gradient of the local objective function is L_1 -Lipschitz continuous.

$$\left\| \nabla \ell_{t_2} - \nabla \ell_{t_2} \right\|_2 \le L_1 \left\| w_{i,t_1} - w_{i,t_2} \right\|_2, \forall t_1, t_2 > 0, i \in \{1, 2, \dots, m\}.$$
 (10)

This also implies the following quadratic bound:

$$\ell_{t_1} - \ell_{t_2} \le \left\langle \nabla \ell_{t_2}, (w_{i,t_1} - w_{i,t_2}) \right\rangle + \frac{L_1}{2} \left\| w_{i,t_1} - w_{i,t_2} \right\|_2^2, \forall t_1, t_2 > 0, i \in \{1, 2, \dots, m\}. \quad (11)$$

Assumption 2. (Unbiased Gradient and Bounded Variance)The stochastic gradient $g_{i,t} = \ell(w_{i,t})$ is an unbiased estimator of the local gradient for each client. Assuming th at its expectation satisfies the following equation:

$$E_{\xi_i} \sim_{D_i} \left[g_{i,t} \right] = \nabla \ell(w_{i,t}) = \nabla \ell_t, \forall i \in \{1, 2, \dots, m\}, \tag{12}$$

and its variance is bounded by σ^2 :

$$E\left[\left\|g_{i,t} - \nabla \ell_{(w_{i,t})}\right\|_{2}^{2}\right] \le \sigma^{2}.$$
(13)

Assumption 3. (Bounded Expectation of Euclidean norm of Stochastic Gradients). The expectation of the random gradient is bounded by *G*:

$$E\left[\left\|g_{i,t}\right\|_{2}\right] \le G, \forall i \in \{1, 2, \cdots, m\}. \tag{14}$$

Assumption 4. The functions of each feature extraction module, commonly known as embedding functions, are L_2 -Lipschitz continuous.

$$||f_{i}(\phi_{i,t_{1}}) - f_{i}(\phi_{i,t_{2}})|| \le L_{2} ||\phi_{i,t_{1}} - \phi_{i,t_{2}}||_{2}, \forall t_{1}, t_{2} > 0, i \in \{1, 2, \dots, m\}.$$

$$(15)$$

We can obtain theoretical results for non-convex problems if the above assumption holds. In Theorem 1, we provide the expected decrease in each round. We use $e \in \{\frac{1}{2}, 1, 2, \dots, E\}$ to represent local iterations and t to represent global communication rounds. Here, tE represents the time step before global features aggregation, and $tE + \frac{1}{2}$ represents the time step between global features aggregation and the first iteration of this round.



Theorem 1. (One-round deviation) Let Assumption 1 to 4 hold. For an arbitrary client, after every communication round, we have,

$$\left[\left\| \ell_{(t+1)E + \frac{1}{2}} \right\| \right] \leq \ell_{tE + \frac{1}{2}} - \left(\eta - \frac{L_1 \eta^2}{2} \right) \sum_{e = \frac{1}{2}}^{E-1} \left\| \nabla \ell_{tE+e} \right\|_2^2 + \frac{L_1 E \eta^2}{2} \sigma^2 + \lambda L_2 \eta EG. \tag{16}$$

Theorem 1 indicates the deviation bound of the local objective function for an arbit rary client after each communication round. Convergence can be guaranteed when the re is a certain expected one-round decrease, which can be achieved by choosing appropriate η and λ .

Corollary 1. (Non-convex pFedPM convergence). The loss function ℓ of an arbitrary client monotonously decreases in every communication round when

$$\eta_{e} < \frac{2(\sum_{e=\frac{1}{2}}^{e} \left\| \nabla \ell_{tE+e} \right\|_{2}^{2} - \lambda L_{2}EG)}{L_{2}EG}, \tag{17}$$

where $e = \{\frac{1}{2}, 1, 2, \dots, E\}$ and

$$\lambda_{t} < \frac{\left\| \nabla \ell_{tE+\frac{1}{2}} \right\|_{2}^{2}}{L_{2}EG}.$$
(18)

Thus, the loss function converges. Corollary 1 guarantees that the expected bias of the loss function is negative, ensuring the convergence of the loss function. We can fur ther ensure the convergence of the algorithm by choosing appropriate learning rates η and importance weights λ .

5 Experiments

Datasets: We evaluate our method on three classification tasks:

- Digits [23] includes four domains: MNIST (M), USPS (U), SVHN (SV), and SYN (SY) with 10 categories (digit numbers from 0 to 9).
- PACS [24] data set is a domain adaptive image dataset, including 4 domains: photo s, art paintings, cartoons, and sketches. Each field contains 7 categories.

Local models: For these three classification tasks, we use the classical ResNet18 [2 5] model as our base model, and all methods use the same network architecture to mak e fair comparisons across different tasks.

Baselines of FL: We investigate the performance of our method PFPL under mixe d heterogeneous conditions and compare it with baselines, including FedAvg, Local. I

n addition, some FL methods in single-domain scenarios are also included. Feature dis tribution skewed: FedBN [12], FRaug [17]. Label distribution skewed: FedProto [15], Ditto [26], APFL [27], FedRod [21], FedKD [28].

Mixed heterogeneous setting: This paper considers a heterogeneous scenario whe re the label distribution is skewed and the feature distribution is skewed. We borrow t he concept of n-way, k-short from less sample learning, which n controls the number o f classes on the client side and k controls the number of training instances per class. T o simulate the label distribution skewed, we stochastic change the values of n and k fo r each client side. For the feature distribution skewed, we stochastic assign instance da ta from different domains to the client side. The final client-side data only has data for individual category labels and is sourced from different domains, albeit with overlap.

Implementation Details: We implement the comparison of PFPL and general base line methods in PyTorch. We use 20 client sides for all data sets. For Digits and PAPC Dataset, the average number of categories n for local clients is set to 3, 4, 5, and for O ffice-31 [29] Dataset, the average number of categories n for local clients is set to 10, 15, 20. And the number of each class in each client side is initially set to 100%. To ma ke a fair comparison, we follow the same settings. For all methods, we use an SGD op timizer with a learning rate of lr = 0.01. The corresponding weight decay is e^{-5} and the momentum is 0.9. The training batch size is 4, and we communicate epoch for E = 100 and the local update wheel T = 1.

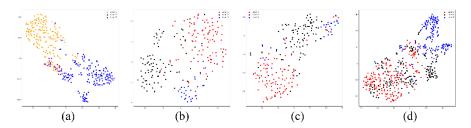


Fig. 3. t-SNE visualization of the prototype generated by the PFPL method. We consider clients from four different domains in the PACS dataset, corresponding to the (a),(b),(c) and (d) in the picture, and the number of classes for each client is uniformly set to n = 3.

PFPL under varying α :As shown in Equation (4), in the server-level personalize d prototype aggregation stage, a controls the weight of the local prototype. As shown in Fig.3, in the range of 0-1, the optimal values of three different data sets a are 0.3, 0.5, and 0.6.

The model performance under the number of classes n of different clients: Tab le 1 reports the average test accuracy for all clients. It can be seen that PFPL has the hi ghest accuracy in most cases among FL under different n controls.



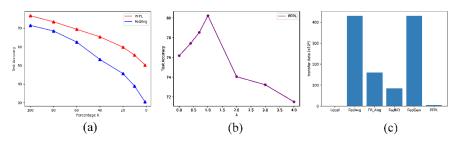


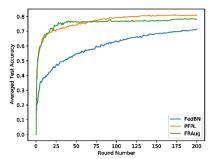
Fig. 4. (a) Average test accuracy of PFPL and FedAvg on PACS with varying numbers of samples in each class. (b) Model accuracy corresponding to different λ . (c) Comparison of the number of parameters transferred in each round of global iteration.

Table 1. Results for the Digits dataset on different algorithms.

Algo-	Acc n=3					Acc n=4	Acc n=5	Rounds
rithms	MNIST	USPS	SVHN	SYN	AVG	AVG	AVG	Roulius
Local	98.32	93.64	85.42	53.18	91.15	92.17	92.86	0
FedAvg	98.64	92.17	86.35	54.16	87.56	88.42	88.75	200
Ditto	96.35	90.86	85.44	53.12	86.74	87.14	87.56	200
APFL	98.42	91.24	86.14	53.42	87.98	88.58	89.43	200
FedRod	95.58	90.33	85.18	52.47	85.61	86.47	86.21	200
FedKD	97.74	92.58	83.22	54.16	86.32	87.36	88.22	200
FedGen	96.35	91.42	82.96	54.88	85.48	86.44	87.64	200
FedBN	98.56	93.10	86.37	53.35	87.54	88.63	89.48	200
FRAug	98.17	92.58	84.51	52.67	93.64	94.51	95.16	200
FedProto	98.42	93.17	88.15	54.42	93.16	94.16	94.23	200
PFPL	98.68	93.94	87.63	60.28	94.75	95.84	96.17	200

Scalability of PFPL on varying number of samples: Fig.4a shows that PFPL can scale to scenarios with fewer samples available on clients. The test accuracy consiste ntly decreases when there are fewer samples for training, but PFPL drops more slowly than FedAvg as a result of its adaptability and scalability on various data sizes.

PFPL under varying λ : Fig.4b shows the change in performance at different values of λ in Equation (7). We specify the initial range of λ at [0,4] and extract a set of values from it. We record the average test accuracy of the PAPC data set, K = 100%, n = 4, and the distance loss of the prototype. In this case, as λ increases, the original distance loss (regularizer) decreases, while the average test accuracy decreases sharply afte r λ = 1, and finally we take the optimal value of λ as 1.



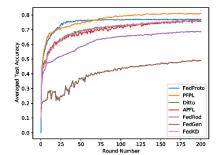


Fig. 5. Precision comparison between PFPL and a single heterogeneous personalized federated learning method in mixed heterogeneous scenarios. (a) indicates the skewed feature distribution scenario, and (b) indicates the skewed label distribution scenario.

PFPL communication efficiency comparison: Fig.4c depicts the number of para meters to be transmitted by each client in each communication round. In comparison with the classical approach, our method transmits the minimal number of parameters in each round, thereby effectively minimizing the volume of communication throughout the entire communication round, lowering the communication cost and enhancing the transmission efficiency.

Performance of PFPL compared to the single-domain FL method: As shown in Fig.5, PFPL achieves higher accuracy than the FL method in single heterogeneous sc enarios with skewed label distributions and skewed feature distributions. We suspect t hat this is due to the fact that previous FL methods focused on solving the heterogeneous federation problem in single scenarios and ignored other heterogeneous scenarios, r esulting in lower performance in mixed heterogeneous scenarios.

6 Conclusion

In this paper, we explore the personalized federated learning PFPL for handling mixed heterogeneous scenarios. Our work introduces prototype as a communication standar d. We use prototype (prototype-like representation) to learn knowledge of different do mains and stable convergence goals by generating specific personalized prototypes for different client sides and introducing personalized prototype consistency during the lo cal update phase. Ultimately, our method achieves higher accuracy than single-scenari o heterogeneous federated learning methods.

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